

Using an ECR Framework to Characterize Problem Difficulty

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Research Questions

How do students' and instructors' estimation of difficulty compare?

How does the complexity of a problem affect its perceived difficulty?

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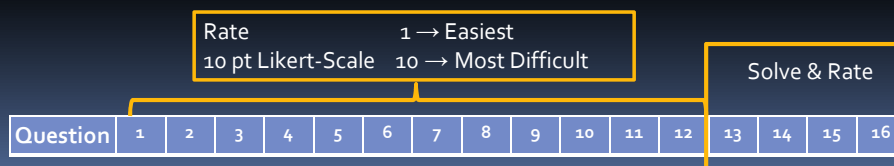
Project

- Developed a **Survey of Problem Difficulty Estimation (SPDE)**
- SPDE → Students & Instructors
- Developed a **rubric** for textbook style physics problems.
- **Correlation** between SPDE and the rubric

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SPDE (Survey of Problem Difficulty Estimation)

- 16 Work & Mechanical Energy problems
 - ✓ Halliday, Resnick & Walker, 7th Ed.
 - ✓ Context Rich Problems
 - ✓ Numbers, symbols, equations, graphs, pictures
- Online Delivery



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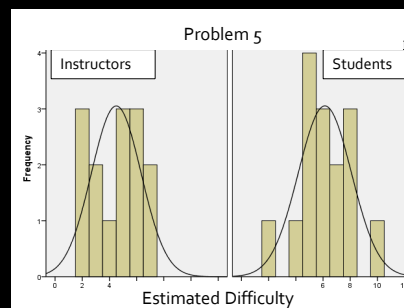
SPDE → Students & Instructors

15 Freshman Physics Majors

"Estimate the difficulty"

14 Instructors

"Estimate the difficulty for a student"



Independent Samples Mann-Whitney U Test

	P ₁	P ₂	P ₃	P ₄	P ₅	P ₆	P ₇	P ₈	P ₉	P ₁₀	P ₁₁	P ₁₂	P ₁₃	P ₁₄	P ₁₅	P ₁₆
P-value	.71	.85	.96	.10	.04	.14	.01	.24	.16	.79	.01	.01	.00	.91	.55	.00
Median Stu	2	2	2	5	6	5	4	6	6	6	5	5	4	6	6	3
Median Inst	2	2	2	4	5	6	6	7	4.5	6	7	7	7	5	5	6

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Rubric - ECR Framework

Exposition

Liz is a post-doc in the Kansas State physics education research group.

Complication

The physics education community is unaware of the work that she is doing at Kansas State University.

Resolution

Liz goes to the AAPT 2010 Winter Meeting and gives a well-received talk about her research.

Baggett, 1979

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ECR & Physics Problems

How much potential energy is stored in a spring with spring constant $k = 170 \text{ N/m}$ when it is compressed 5 cm ?

Exposition

Spring with $k = 170 \text{ N/m}$
compressed 5 cm

Complication

Complication
Resolution

Calculate the potential energy

What physics idea to use?
Definition of potential energy for linear spring
 $U = \frac{1}{2}kx^2$

Complication
Resolution

Which numbers go with which variables?
 $k=170 \text{ N/m}$, $x= 5 \text{ cm}$

Resolution

Value of the potential energy

3 CR Pairs

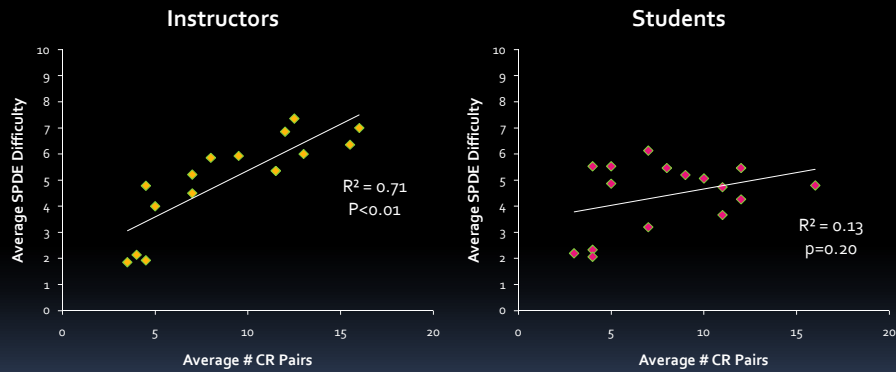
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Reliability

Problems	Reliability
Solved Textbook Examples Halliday, Resnick & Walker (7 th ed) Knight (2004)	0.78
SPDE Problems	0.72

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ECR & SPDE Correlation



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Conclusions

- Student and instructor estimation of problem difficulty can be quite different
 - ✓ No global trend
 - ✓ Context rich problems → students estimate as easier
- Instructors' difficulty estimations rely more strongly on the number of steps in the solution than do students'.
 - Compare correct response rate with difficulty estimation & ECR score
 - Other physics topics

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Thank You

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SPDE (Survey of Problem Difficulty Estimation)

- Online survey
- 16 Work & Mechanical Energy problems
 - ✓ Halliday, Resnick & Walker, 7th Ed.
 - ✓ Context Rich Problems
 - ✓ Numerical, equations, graphs, pictures

Rank 1 → Easiest
10 pt Likert-Scale 10 → Most Difficult

Solve & Rank

Position:	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Winter	Q2	Q11	Q6	Q7	Q8	Q1	Q9	Q12	Q15	Q3	Q16	Q10	Q13	Q14	Q4	Q5
Spring	Q3	Q5	Q16	Q7	Q10	Q1	Q11	Q12	Q13	Q4	Q14	Q6	Q8	Q9	Q2	Q15
Summer	Q13	Q3	Q7	Q4	Q14	Q5	Q10	Q9	Q8	Q2	Q12	Q15	Q6	Q11	Q1	Q16
Fall	Q11	Q2	Q8	Q5	Q1	Q15	Q6	Q9	Q13	Q14	Q16	Q4	Q7	Q12	Q10	Q3

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What makes a physics problem difficult?

Characteristics of the Problem

- ✓ Amount of **information** given in the problem
- ✓ How **information** given in the problem
- ✓ Amount of **math** manipulation involved in the solution
- ✓ Which **physics ideas** are involved in the solution

Interaction Between Problem & Solver

- ✓ What **knowledge** does the solver possess that **can be used** to solve the problem?
- ✓ What **knowledge** does the solver possess that they **see as relevant** to the problem?
- ✓ How **familiar** is the context?